

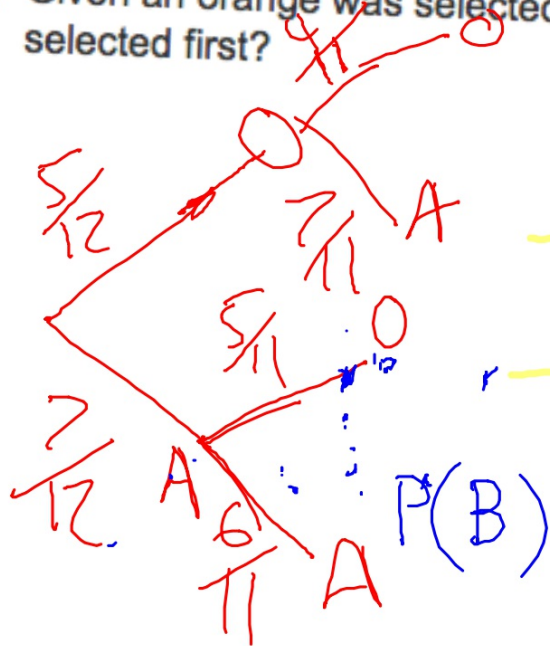
## IB Math Studies BELL WORK

A bowl of fruit contained 5 oranges and 7 apples a child selected two pieces of fruit to take to school.

- (i) Draw a tree diagram to show the possible choices made
- (ii) Calculate the probability of selecting an orange?
- (iii) Given an orange was selected, what is the probability that a apple was selected first?

B: An orange was selected

A: apple selected 1st



$$\frac{20}{132}$$

$$\frac{35}{132}$$

$$\frac{35}{132}$$

$$\frac{90}{132} = \frac{15}{22}$$

$$P(A|B) = \frac{P(A \cap B)}{P(B)}$$

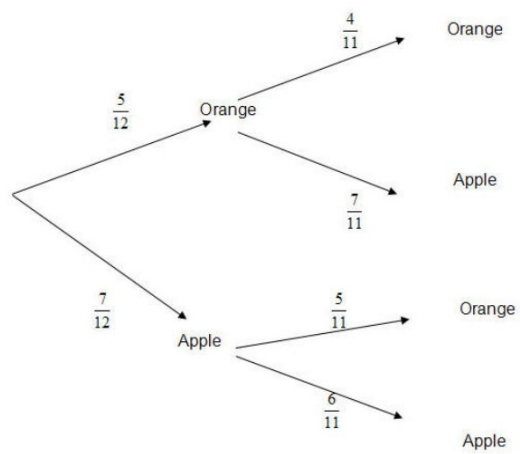
$$\frac{\frac{35}{132}}{\frac{90}{132}}$$

$$P(A|B) = \frac{P(A \cap B)}{P(B)}$$

$$P(\text{apple 1st} | \text{orange}) = \frac{\frac{35}{\cancel{132}}}{\frac{90}{\cancel{132}}}$$

$$\frac{35}{90} = \frac{7}{18}$$

(i)



(ii) There are three ways of getting an orange

*(orange first  $\cap$  apple second) or (apple first  $\cap$  orange second) or*

$$\textit{(orange first  $\cap$  orange second)} = \left(\frac{5}{12} \times \frac{7}{11}\right) + \left(\frac{7}{12} \times \frac{5}{11}\right) + \left(\frac{5}{12} \times \frac{4}{11}\right) = \frac{15}{22}$$

(iii) We now need to use the conditional probability formula

$$P(A|B) = \frac{P(A \cap B)}{P(B)} \quad \text{where } P(B) = \frac{15}{22} \quad \text{and} \quad P(A \cap B) = \frac{7}{12} \times \frac{5}{11} = \frac{35}{132}$$

$$\text{So } P(A|B) = \frac{\frac{35}{132}}{\frac{15}{22}} = \frac{7}{18}$$

# Chapter 19

## Unfamiliar functions

**Syllabus reference:** 6.5, 6.6, 6.7

- Contents:**
- A** Properties of functions
  - B** Asymptotes
  - C** Combined power functions
  - D** Combined functions
  - E** Where functions meet

## Important features of graphs:

The main features we are interested in are:

- the axes intercepts where the graph cuts the  $x$  and  $y$ -axes
- turning points (local maxima and local minima)
- the domain and range
- values of  $x$  where the function does not exist
- the presence of asymptotes, or lines that the graph approaches.

→ Calc "zero"  
value  $x=0$   
Calc: Max / min

**Graphs to Know and Love**

**Coolmath<sup>®</sup>.com**

**Know them and be a happy student...**

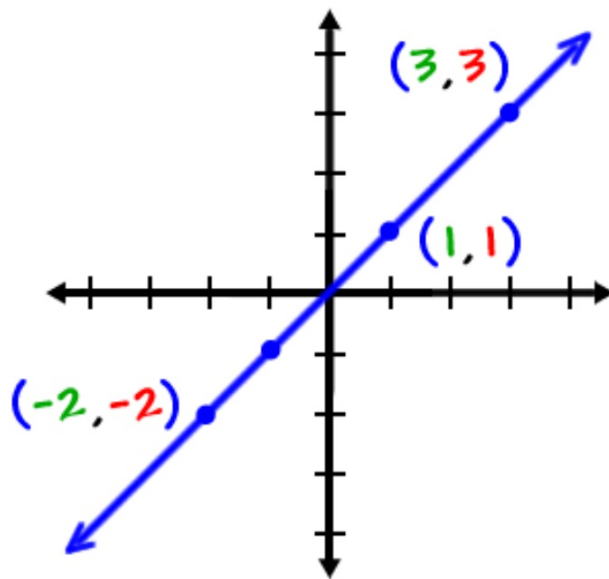
**Love them and be a happy geek!**

## Graphs to Know and Love

First, here's a special line guy that you've probably seen before... I call him

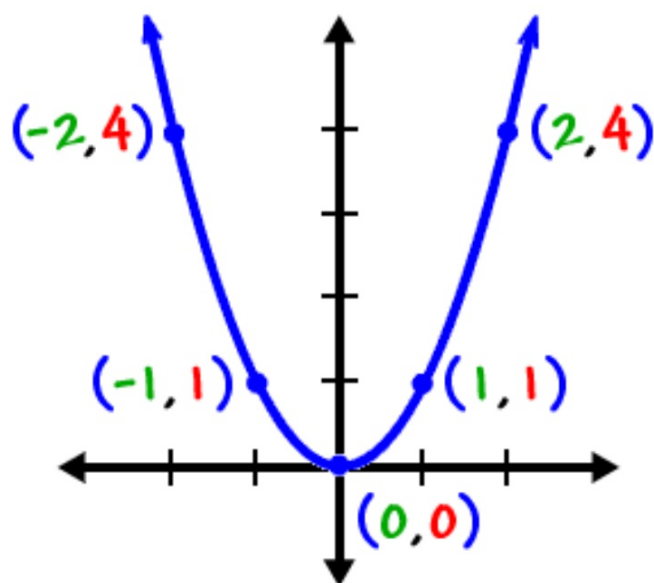
**45° Line Guy:**

$$y = x$$



And you probably already love **Standard Parabola Guy**:

$$y = x^2$$



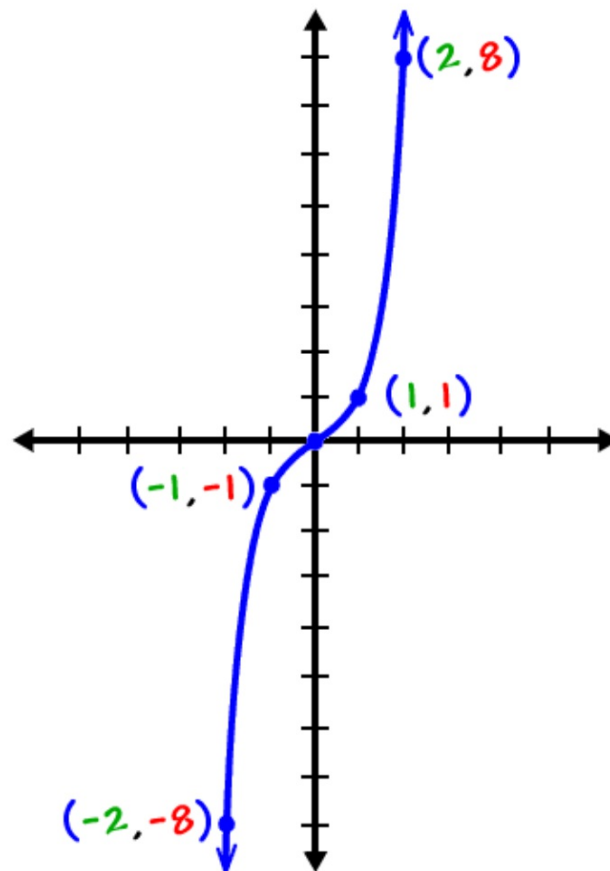


Here are some that may be new to you:

### The Disco Graph:

$$y = x^3$$

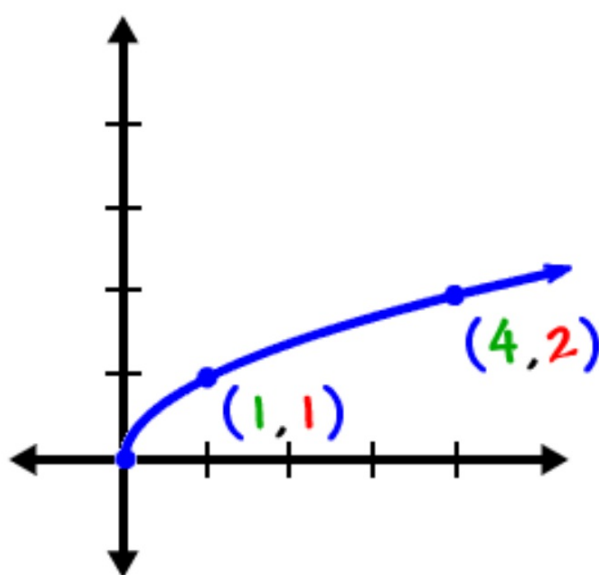
You know...  
John Travolta?  
That pose?



**Square Root Guy:**

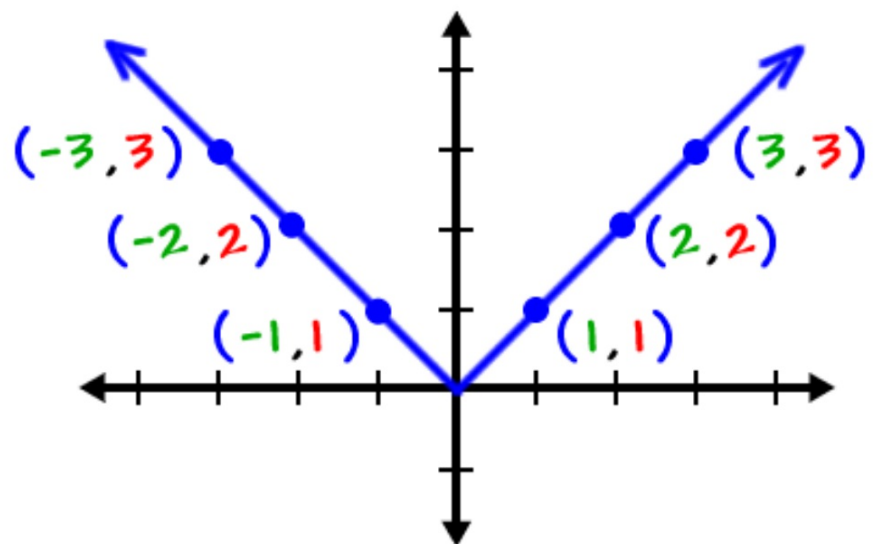
$$y = \sqrt{x}$$

It's just half of  
a parabola lying  
on its side.



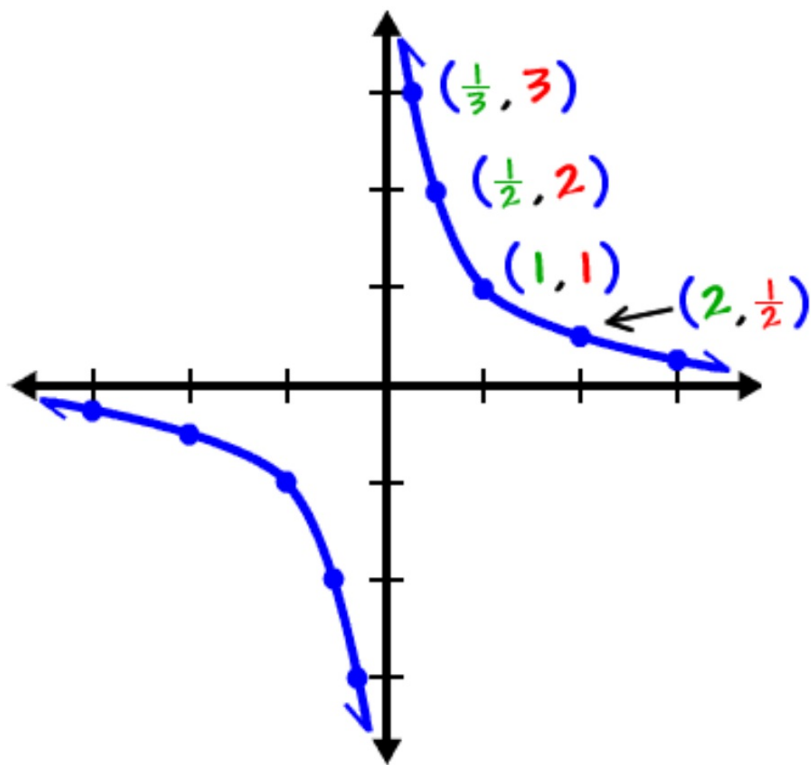
**Absolute Value Guy (or V guy):**

$$y = |x|$$



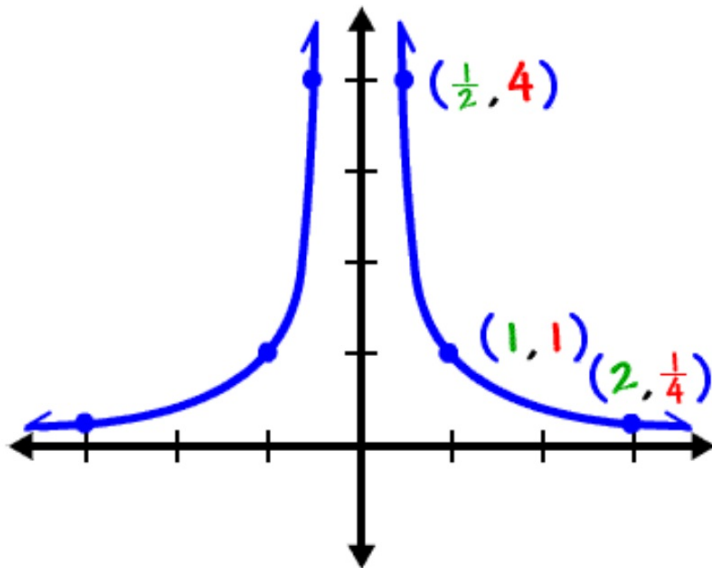
## The Flying Butterfly:

$$y = \frac{1}{x}$$



## The Volcano:

$$Y = \frac{1}{x^2}$$



So, there's the list.



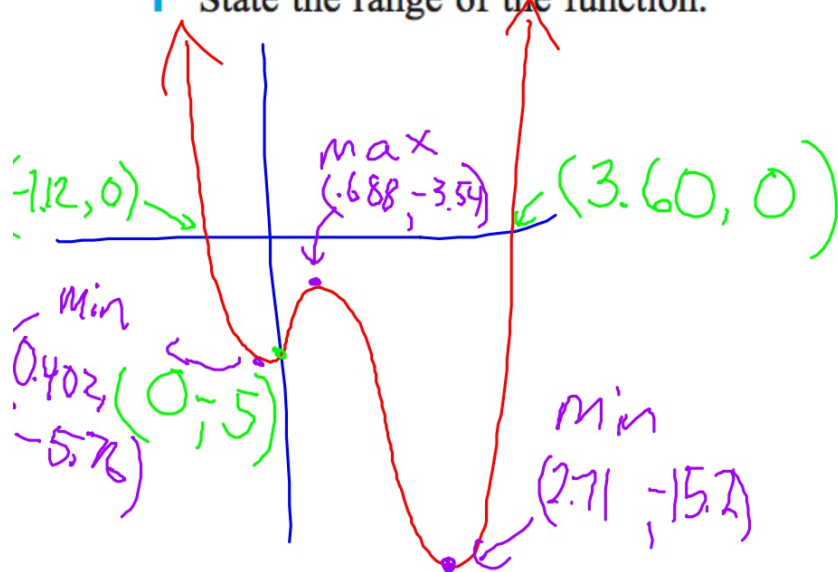
Know them,  
and more importantly...

**LOVE THEM!**



Consider the function  $y = x^4 - 4x^3 + x^2 + 3x - 5$ .

- By first graphing the function on your calculator, sketch the function.
- Find the axes intercepts.
- Find the coordinates and nature of any local maxima or minima.
- Discuss the behaviour of the function as  $x \rightarrow \infty$  and  $x \rightarrow -\infty$ .
- Add to your graph in **a** the key features found in **b** and **c**.
- State the range of the function.



Range

$$\{y \mid y \geq -15.2\}$$

Exercise 19 A # 1, 3 a, c, e