

IB Math Studies 1 BELL WORK

A field is 91.4 m long and 68.5 m wide.

- a) Calculate the area of the field in  $\text{m}^2$ .
- b) Calculate the area of the field in  $\text{cm}^2$ .
- c) Express your answer to (b) in the form  $a \times 10^k$  where  $1 \leq a < 10$  and  $k$  is an integer

IB Math Studies 1 BELL WORK

Show that the following are rational numbers:

1. 0.68385  $\frac{68385}{100000}$

2.  $0.4141414141414141\dots = x$

$0.7777\dots$

$$\frac{41}{99}$$

$$41.\overline{41} = 100x \frac{7}{9}$$
$$41 + x$$

# Chapter

# 3

## Laws of algebra

- A** Laws of exponents
- B** The distributive law
- C** The product  $(a + b)(c + d)$
- D** Difference of two squares
- E** Perfect squares expansions
- F** Further expansion

**A****LAWS OF EXPONENTS**

The following are **laws of exponents** for  $m, n \in \mathbb{Z}$ :

$$a^m \times a^n = a^{m+n}$$

To **multiply** numbers with the **same base**, keep the base and **add** the exponents.

$$\frac{a^m}{a^n} = a^{m-n}, \quad a \neq 0$$

To **divide** numbers with the **same base**, keep the base and **subtract** the exponents.

$$(a^m)^n = a^{m \times n}$$

When **raising a power to a power**, keep the base and **multiply** the exponents.

$$(ab)^n = a^n b^n$$

The power of a product is the product of the powers.

$$\left(\frac{a}{b}\right)^n = \frac{a^n}{b^n}, \quad b \neq 0$$

The power of a quotient is the quotient of the powers.

$$a^0 = 1, \quad a \neq 0$$

Any non-zero number raised to the exponent zero is 1.

$$a^{-n} = \frac{1}{a^n} \quad \text{and} \quad \frac{1}{a^{-n}} = a^n \quad \text{and in particular} \quad a^{-1} = \frac{1}{a}, \quad a \neq 0.$$

Simplify

**a**  $k^4 \times k^2$

**b**  $5^2 \times 5^6$

**c**  $5^9 \div 5^6$

**d**  $\frac{m^{10}}{m^4}$

**e**  $(7^6)^d$

**f**  $(g^k)^8$

**g**  $3^2 \times 3^7 \times 3^4$

**h**  $(j^4)^{3x}$

**i**  $11^6 \times 11$

**j**  $\frac{z^7}{z^{4t}}$

**k**  $(13^c)^{5d}$

**l**  $w^{7p} \div w$

Simplify

**a**  $k^4 \times k^2$

$$k^6$$

**b**  $5^2 \times 5^6$

$$5^8$$

**c**  $5^9 \div 5^6$

$$5^3$$

**d**  $\frac{m^{10}}{m^4}$

$$m^6$$

**e**  $(7^6)^d$

$$7^{6d}$$

**f**  $(g^k)^8$

$$g^{8k}$$

**g**  $3^2 \times 3^7 \times 3^4$

$$3^{13}$$

**h**  $(j^4)^{3x}$

$$j^{12x}$$

**i**  $11^6 \times 11$

$$11^7$$

**j**  $\frac{z^7}{z^{4t}}$

$$z^{7-4t}$$

**k**  $(13^c)^{5d}$

$$13^{5cd}$$

**l**  $w^{7p} \div w^1$

$$\frac{w^{7p}}{w^1} = w^{7p-1}$$

Express in simplest form with a prime number base:

**a** 32

**b** 49

**c**  $25^3$

**d**  $9^{t+2}$

**e**  $32^{2-r}$

**f**  $\frac{81}{3y+1}$

Express in simplest form with a prime number base:

**a** 32

$$2^5$$

**b** 49

$$7^2$$

**c**  $25^3$

$$5^6$$

**d**  $9^{t+2}$

$$3^{2t+4}$$
$$(3^2)^{t+2}$$

**e**  $32^{2-r}$

$$(2^5)^{2-r}$$
$$2^{10-5r}$$

**f**  $\frac{81}{3^{y+1}}$

$$\frac{3^4}{3^{y+1}}$$

$$3^{3-y}$$

$$3^{4-(y+1)}$$



Write without negative exponents:

**a**  $5n^{-1}$

**f**  $m^{-1}n$

**c**  $\left(\frac{5}{n}\right)^{-1}$

**d**  $\left(\frac{n}{5}\right)^{-2}$

Write without negative exponents:

**a**  $5n^{-1}$

$$\frac{5}{n}$$

**f**  $m^{-1}n$

$$\frac{n}{m}$$

**c**  $\left(\frac{5}{n}\right)^{-1}$

$$\frac{n}{5}$$

**d**  $\left(\frac{n}{5}\right)^{-2}$

$$\frac{25}{n^2}$$

Simplify using the laws of exponents:

**i**  $5s^2t \times 4t^3$

**j**  $\frac{(k^4)^5}{k^3 \times k^6}$

**k**  $\frac{12x^2y^5}{8xy^2}$

Simplify using the laws of exponents:

**i**  $5s^2t \times 4t^3$

$20s^2t^4$

**j**  $\frac{(k^4)^5}{k^3 \times k^6}$

$k^{11}$

**k**  $\frac{12x^2y^5}{8xy^2}$

$\frac{3xy^3}{2}$

Complete Exercise

3 A.2 all numbers d-g.

Expand and simplify:

$$(3 - 2x)^2$$

$$(3 - 2x)(3 - 2x)$$

$$9 - 6x - 6x + 4x^2 \quad 4x^2 - 12x + 9$$

$$(3x + 1)(3x - 1) + (x - 7)^2$$

$$(2 + x)(5 - x)(3x + 1)$$

Expand and simplify:

$$(3 - 2x)^2$$

Expand and simplify:

$$(3x + 1)(3x - 1) + (x - 7)^2$$



Expand and simplify:

$$(2 + x)(5 - x)(3x + 1)$$

Assignment:

Review Set 3B